## SCHWARZSCHILD RADIUS

This can be obtained by equating the Newtonian escape speed  $v_N$  to the speed of light c. To obtain  $v_N$  set the initial kinetic energy  $KE = \frac{1}{2}mv_N^2$  of a mass m equal to the change in potential energy  $PE = GMm/R_s$  in going from a distance  $R_s$  (the Schwarzschild radius) to an infinite distance away from a mass M:

$$\frac{1}{2}mv_N^2 = \frac{1}{2}mc^2 = GMm/R_s \Longrightarrow R_s = 2GM/c^2.$$
(1)

The term  $\frac{1}{2}mc^2$  is not relativistic because of the Newtonian derivation. Nevertheless eq. (1) is the same as the general relativity (GR) result(!).

The Schwarzschild radius for a Planck mass  $m_P = (\hbar c / G)^{1/2}$  is  $R_s = (2Gm_P / c^2)$ =  $2(\hbar G / c^3)^{1/2}$ , twice the Planck length.